

Raith (2003): Competition, Risk and Managerial Incentives

Key intuition:

Consider the profit function of a firm

$$\pi_i = (p_i - c_i)q(p_i, \bar{p}_{j \neq i})$$

where  $\bar{p}_{j \neq i}$  is a vector of prices of all other firms.

Firm  $i$  chooses  $p_i$  to maximize  $\pi_i$ .

Consider now the effect of a cost reduction. Using the envelope theorem, this is given by

$$\frac{d\pi_i}{dc_i} = -q(p_i, \bar{p}_{j \neq i}).$$

Thus, in equilibrium, the benefit of cost reduction is positively related to the equilibrium output.

Raith considers 3 ways in which competition can increase. Importantly, the number of firms is not one of these, as it is an endogenous variable in a free-entry/exit equilibrium. The incentives such changes in competition create are related to whether, in equilibrium, output is higher or lower.

- Greater product substitutability: In free entry equilibrium this leads to lower  $N$  but higher  $q$ . So incentives for cost reduction increase.
- Change in market size: new firms enter and each firm also produces more. So incentives for cost reduction increase.
- Decrease in entry costs: New firms enter and firm-level output falls, leading to lower incentives for cost reduction.

Consider the following demand curve:

$$p_i = a - q_i - b \sum_{j \neq i} q_j$$

$$p_j = a - q_j - b \sum_{j \neq k} q_k$$

Firms compete in prices. We can show the following:

- $\pi_i = \frac{(1-b)(1+(n-2)b)(a-c)^2}{(1+(n-1)b)(2+(n-3)b)^2} - f = 0$ . (free-entry equilibrium condition)
- $q = (a-c) \frac{bn-2b+1}{(1+(n-1)b)(2+(n-3)b)} = \sqrt{\frac{(1+(n-2)b)}{(1+(n-1)b)} \frac{f}{1-b}}$

The last relationship shows that with entry cost and degree of substitution constant, output and the number of firms are positively related (both increase in the industry demand parameter  $a$ ).

Notice:

- $\frac{d\left(\frac{(1-b)(1+(n-2)b)(a-c)^2}{(1+(n-1)b)(2+(n-3)b)^2}\right)}{da} > 0$
- $\frac{d\left(\frac{(1-b)(1+(n-2)b)(a-c)^2}{(1+(n-1)b)(2+(n-3)b)^2}\right)}{dn} = b(a-c)^2 \frac{b-1}{(bn-b+1)^3} (bn-3b+1) < 0$
- Hence, for the free entry condition hold to hold,  $\frac{dn}{da} > 0$ .
- Since  $q = \sqrt{\frac{1+(n-2)b}{1+(n-1)b} \left(\frac{f}{1-b}\right)}$ , differentiating, we get  $\frac{d\left(\frac{1+(n-2)b}{1+(n-1)b}\right)}{dn} = \frac{b^2}{(bn-b+1)^2} > 0$ .
- Hence,  $\frac{dq}{da} > 0$ .

Also, clearly,  $\frac{dn}{df} < 0$ . Moreover,

- $\frac{1+(n-2)b}{1+(n-1)b} \left(\frac{f}{1-b}\right) = \frac{(1+(n-2)b)^2(a-c)^2}{(1+(n-1)b)^2(2+(n-3)b)^2} = \left(\frac{1+(n-2)b}{(1+(n-1)b)(2+(n-3)b)}\right)^2 (a-c)^2$ .
- Hence,  $q = \left(\frac{1+(n-2)b}{(1+(n-1)b)(2+(n-3)b)}\right) (a-c)$ .
- Differentiating,  $\frac{d\left(\frac{1+(n-2)b}{(1+(n-1)b)(2+(n-3)b)}\right)}{dn} = \frac{b^2}{(bn-b+1)^2} > 0$ .
- Since  $\frac{dn}{df} < 0$ , it follows that  $\frac{dq}{df} < 0$ .

Finally,

- $\frac{d\left(\frac{(1-b)(1+(n-2)b)(a-c)^2}{(1+(n-1)b)(2+(n-3)b)^2}\right)}{db} = -\frac{(a-c)^2}{(bn-b+1)^3} (n-b+bn^2-2bn+1)$   
 $= -\frac{(a-c)^2}{(bn-b+1)^3} (1-b+n(1+bn-2b)) < 0$ .

• Hence, higher  $b$  leads to lower  $n$ . Moreover,

- $\frac{d\left(\frac{1+(n-2)b}{(1+(n-1)b)(2+(n-3)b)}\right)}{db} = -\frac{1}{(bn-b+1)^2} < 0$ .

Thus, higher  $b$  leads to lower  $n$ , which lowers  $\frac{1+(n-2)b}{(1+(n-1)b)(2+(n-3)b)}$ . It also directly lowers  $\frac{1+(n-2)b}{(1+(n-1)b)(2+(n-3)b)}$ . Thus,  $q$  falls as  $b$  increases.